Methodology for Management of Power System Emergency Situations



GRID



Blackout: not so unusual events ... & correlated



Power Grid infrastructure is highly vulnerable to targeted terrorism attacks

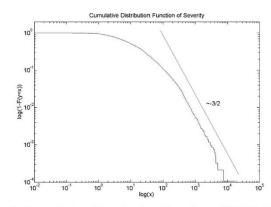
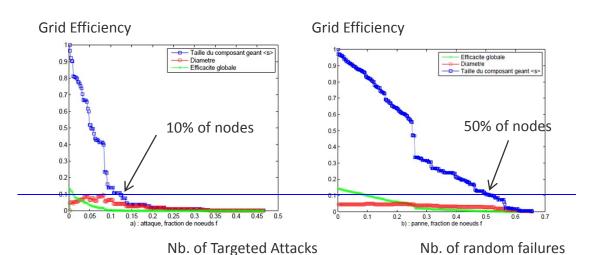


Fig. 9. Cumulative Distribution Function of DNS (KWh)



Experience from ISO/TSO Colombia:

We particularly coordinate the operation with the army in conflict zones and also establish for the regions which are under attack an analysis of contingency n-2 or n-3.



Statistical Power Flow Model: a way to quantify risk

Power Grid

DC/AC Power Flow + optimization

Power Grid + random events

+ Statistical Estimation

Improvements in operating policies, maintenance, equipment, controls, ...

+ Decision support Feedback

Self Organized Criticality – Power Flow model



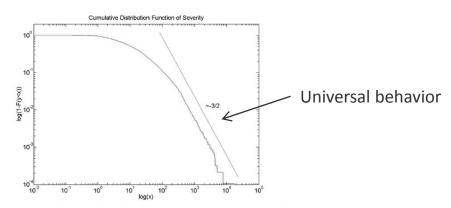


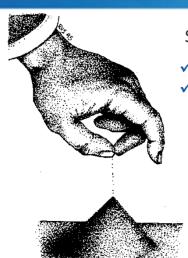
Fig. 9. Cumulative Distribution Function of DNS (KWh)

To reproduce "the life of a power network" over a large sequence of events with a SOC phenomenon

- ✓ 1 fast dynamic, i.e. avalanche phenomena (sequence of events, time resolution: second, minute)
- √ 1 slow dynamic (sequence of events, time resolution : day)



Self-Organized Criticality (SOC)



Sandpile model: 2 dynamics & 2 opposing forces

P. Bak, 1987 I. Dobson, 2000

- slow dynamic: continuous pouring of sand
- fast dynamic (avalanche)
 - oscillating variations of the slope of the sandpile
 - avalanche phenomenon to reach a new equilibrium status: Self Organized Criticality

Analogy between Sandpile and Electrical Grid dynamics

Power system	Variables	Sandpile
fractional overloads	system state	gradient profile
load increase	driving force	addition of sand
line improvements	relaxing force	gravity
line limit or outage	event	sand topples
cascading lines	cascade	avalanche

The grid is a dynamic system, managed by two opposing forces (load plan and "response to incident"), in the critical regime or not (subcritical, critical, super-critical)

The power law behaviour observed experimentally finds its origin in this competition (universal behaviour)

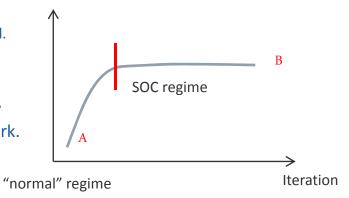


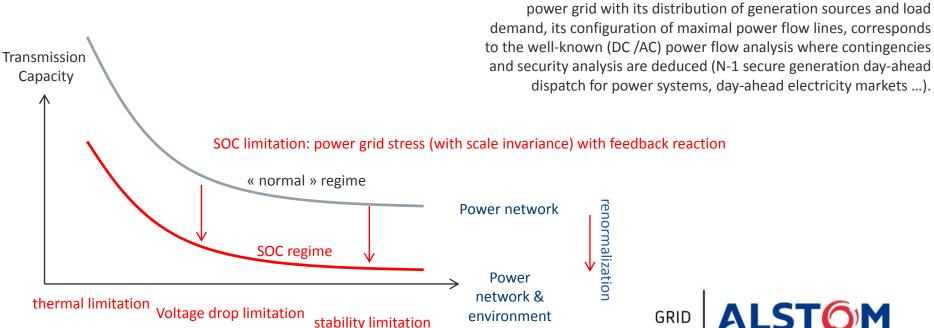
SOC regime limitation

SOC regime:

- ✓ power grid interacts with its surrounding and is close to its limits operating condition
- ✓ feedback reaction to any dysfunction can be operational policy control (control room), human intervention, maintenance operations, planning policy ... and can be quantified.

To reach the SOC regime: put the power grid under maximum stress where any random event can produce a minor failure or a major failure all over the network.







Statistical Power Flow Model (DC or AC SPFM)

SPFM model is based on a Optimal Power Flow resolution with variables of interest, the evolution of the load (nodes) and the improvement of the network (lines)

Failures or external events are randomly generated (Gaussian or not)

SOC regime limitation:

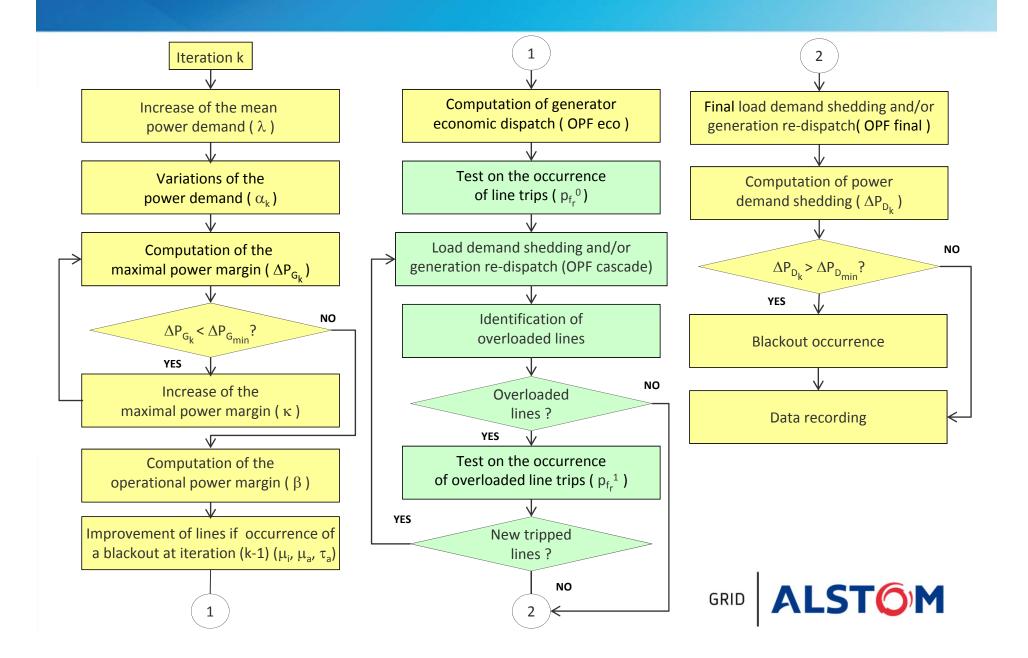
from historical data & generation /load plan

Immediate strategy response & delayed strategy response

Sequence of events



DC SPFM: General Algorithm

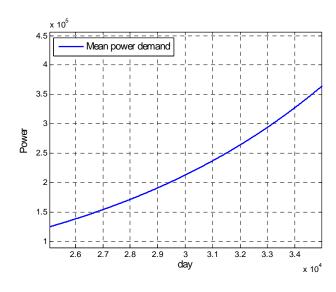


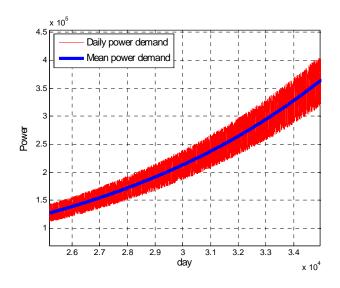
power network evolution: load power demand & power generation capability increase

$$\begin{cases} P_{D_k} = \lambda P_{D_{k-1}} \\ \overline{P}_{D_k} = \alpha_k P_{D_k} \end{cases}$$

Mean power demand evolution

Power demand random variation





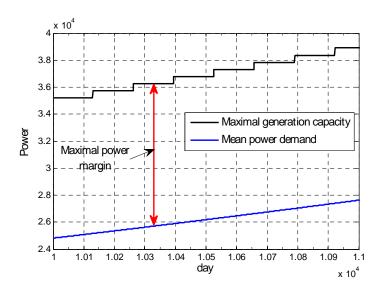


we keep a constant minimal power margin

maximal power margin

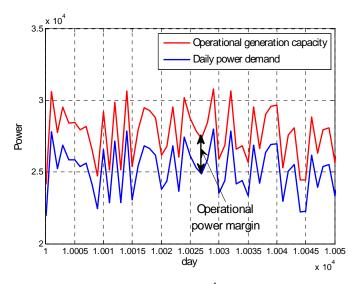
$$\Delta P_{G_k} = \sum_{i=1}^{N_G} P_{G_{\max_i}} - \sum_{j=1}^{N_L} \overline{P}_{D_{k_j}}$$

$$\Delta P_{G_k} \geq \Delta P_G^{\min}$$
 $P_{G_{\max_i}} = P_{G_{\max_i}} + \kappa \sum_{j=1}^{N_L} \overline{P}_{D_{k_j}}$



operational power margin

$$\varepsilon = \beta \frac{\sum_{j=1}^{N_L} P_{D_{k_j}}}{\sum_{i=1}^{N_G} P_{G_{\max_i}}} \qquad P_{G_{\max_{k_i}}}^{op} = \min(\varepsilon P_{G_{\max_i}}, P_{G_{\max_i}})$$





network improvement strategy: feedback actions done by TSO to improve the behavior of network

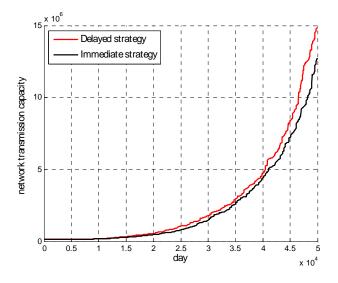
immediate strategy approach (at k + 1)

delayed strategy approach (at $k + \tau_a$)

$$T_{L_{\max_r}} = \mu_i T_{L_{\max_r}}$$

$$\begin{cases} Z_r = Z_r / \mu_i \\ B_{sh_r} = \mu_i B_{sh_r} \end{cases}$$

$$T_{L_{\max_r}} = \mu_a T_{L_{\max_r}} \qquad \begin{cases} Z_r = Z_r / \mu_a \\ B_{sh_r} = \mu_a B_{sh_r} \end{cases}$$



line impedances adapted to be coherent with line maximal flux improvement



Generation economic dispatch is performed in order to determine, on the basis of generation costs, the generator dispatch that will be considered during the following cascade phenomena step.

Optimal Power Flow (OPF eco), to minimize a given cost objective function.

criteria to be minimized

$$J_{eco}(x_{eco}) = \frac{1}{2} P_G^T H P_G + C^T P_G + D$$

optimization variables

$$x_{eco} = [\theta, P_G]^T$$

network physical constraints

$$\begin{cases} P(\theta) - P_G + P_D = 0 \\ T_L(\theta) - T_{L_{\text{max}}} \le 0 \end{cases}$$

optimization variable lower and upper bounds

$$\begin{cases} \theta_{\min} \leq \theta \leq \theta_{\max} \\ P_{G_{\min}} \leq P_{G} \leq P_{G_{\max}} \end{cases}$$



DC SPFM: Fast dynamics

Cascade phenomena are consequence of initial tripping events occurring in the network (line tripping occurrences). -> could be associated to weather conditions (e.g. storms), network bad maintenance (e.g. line contacting trees, aged components), human errors, network attacks (e.g. terrorism actions), ... initial line tripping events are depending on a given line fault probability introduced through a constant initial fault probability associated to each line.

Line trip initial occurrence

constant initial fault probability

 $p_{f_r}^0$

Overloaded line trip occurrence

line loading rate

 $L_r = \frac{|T_r|}{T_{\max_r}}$

line overloading condition

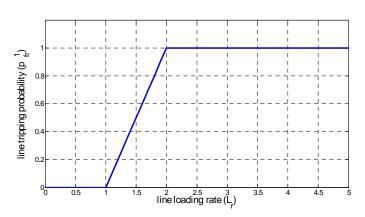
$$L_r \ge L_r^{th}$$

overloaded line fault probability

$$p_{f_r}^1$$

or

$$p_{f_r}^1 = f(L_r)$$



DC SPFM: Fast dynamics

Load power demand shedding and/or generation power re-dispatching process

During cascade phenomena, power flowing through lines cannot be controlled and could be greater than maximal allowed power flows.

As far as one or several lines tripped, it could be necessary to re-dispatch generation power and, potentially, to shed load power demand to assure network stability (OPF)

criteria to be minimized

$$J(x) = \sum_{j=1}^{N_L} \omega_{D_j} (P_{D_{0_j}} - P_{D_j})^2 + \sum_{i=1}^{N_G} \omega_{G_i} (P_{G_{0_i}} - P_{G_i})^2$$

optimization variables

$$x = [\theta, P_G, P_D]^T$$

network physical constraints

$$\begin{cases} P(\theta) - P_G + P_D = 0 \\ T_L(\theta) - T_{L_{\text{max}}} \le 0 \end{cases} \quad \text{or} \quad P(\theta) - P_G + P_D = 0$$

optimization variable lower and upper bounds

$$\begin{cases} \theta_{\min} \leq \theta \leq \theta_{\max} \\ P_{G_{\min}} \leq P_{G} \leq P_{G_{\max}} \\ 0 \leq P_{D} \leq P_{D_{0}} \end{cases}$$



When the cascade phenomena phase ended, we compute the network final power balance (final load power demand shed and/or generation power re-dispatch) taking into account the tripped lines. As far as one or several lines tripped, it could be necessary to re-dispatch generation power and, potentially, to shed load power demand to assure network stability (OPF)

criteria to be minimized

$$J(x) = \sum_{j=1}^{N_L} \omega_{D_j} (P_{D_{0_j}} - P_{D_j})^2 + \sum_{i=1}^{N_G} \omega_{G_i} (P_{G_{0_i}} - P_{G_i})^2$$

optimization variables

$$x = [\theta, P_G, P_D]^T$$

network physical constraints

$$\begin{cases} P(\theta) - P_G + P_D = 0 \\ T_L(\theta) - T_{L_{\text{max}}} \le 0 \end{cases}$$

optimization variable lower and upper bounds

$$\begin{cases} \theta_{\min} \leq \theta \leq \theta_{\max} \\ P_{G_{\min}} \leq P_{G} \leq P_{G_{\max}} \\ 0 \leq P_{D} \leq P_{D_{0}} \end{cases}$$

Power demand shedding event is identified when the amount of shed power demand is greater than a defined shed power demand threshold

$$\Delta P_D = \sum_{j=1}^{N_L} (P_{D_{0_j}} - P_{D_j}) \ge \Delta P_D^{\min}$$



SOC condition

To get a distribution of line maximal capacities which set the power network in maximal stress operating conditions, corresponding to the natural SOC behavior observed from real historical data analysis

A constant ratio between the sum of line power flow maximal capacities and the sum of node load demands

$$\gamma = rac{\displaystyle\sum_{r=1}^{N_B} T_{ ext{max}_r}}{\displaystyle\sum_{j=1}^{N_L} P_{D_j}} = \gamma_{SOC}$$

$$\gamma = \frac{\sum_{r=1}^{N_B} T_{max_r}}{\sum_{j=1}^{N_L} P_{D_j}} = \gamma_{SOC}$$
SOC regime

A constant mean lines loading rate

$$\tau = \frac{\sum_{r=1}^{N_B} \frac{\left| T_r \right|}{T_{\text{max}_r}}}{N_B} = \tau_{SOC}$$

$$\tau = \frac{\sum\limits_{r=1}^{N_{B}} \frac{\left|T_{r}\right|}{T_{\max_{r}}}}{N_{B}} = \tau_{SOC}$$
 SOC regime transient regime

SOC condition setting process

To determine the distribution of line maximal transmission capacities $T_{\mathrm{max}_r}^{\mathit{final}}$

network topology

final power demand set point

final generation power dispatch set point

$$P_{D_{j}}^{\mathit{final}} \ P_{G_{i}}^{\mathit{final}}$$

Define an initial network state

$$P_{D_{j}}^{init} = \frac{P_{D_{j}}^{final}}{r_{P}} \quad P_{G_{i}}^{init} = \frac{P_{G_{i}}^{final}}{r_{P}} \quad T_{\max_{r}}^{init} = \frac{T_{\max_{r}}^{AC}}{r_{T}}$$

$$\text{such that} \quad \gamma_{init} = \frac{\sum_{r=1}^{N_{B}} T_{\max_{r}}^{init}}{\sum_{j=1}^{N_{L}} P_{D_{j}}^{init}} > \gamma_{SOC}$$

$$T_{init} = \frac{T_{\max_{r}}^{finit}}{N_{B}} < \tau_{SOC}$$

Power demand and generation power linear evolution until the final mean power demand is reached

$$P_{D_{k_j}} = P_{D_{k-1_j}} + \Delta P_{D_j}$$

$$P_{G_{k_i}} = P_{G_{k-1_i}} + \Delta P_{G_i}$$

$$P_{G_{\max_{k_i}}} = P_{G_{\max_{k-1_i}}} + \Delta P_{G_{\max_i}}$$

immediate strategy approach (at k+1)
$$T_{L_{\max_r}} = \mu_i \, T_{L_{\max_r}}$$
 delayed strategy approach (at k+ au_a) $T_{L_{\max_r}} = \mu_a \, T_{L_{\max_r}}$

$$T_{L_{\max_r}}^{final} \leq T_{L_{\max_r}}^{AC}$$



Application to day-ahead risk assessment

The main assumption made is that most of information about system behavior can be deduced from the SOC condition setting process, computed for given power demand set point, given generation dispatch set point and given network topology, corresponding to the studied day-ahead network operating conditions

Case of the Colombian Electrical Network, with high voltage (i.e. 110 kV, 220 kV and 500 kV) transport network 392 buses (or nodes), 94 "generator" nodes, 647 lines

3 generation dispatches:

- "Ideal Dispatch" (ID), only economical cost objective as well as areas power balance constraints.

 This dispatch is optimal from an economical point of view. However, it does not consider any network constraints and must be assessed in this sense
- "Network Dispatch" (ND) with network topology constraints, such as line maximal transportation capacities and N-1 contingency, in a simplified DC based approach
- "Coordinated Dispatch", which takes into account additional network requirements (e.g. voltage and stability constraints), while seeking being as close as possible to previous dispatches for minimizing the "cost loss" due to dispatch modification



Application to day-ahead risk assessment

Day 1 characterized by:

A high level of power demand (stressed network)

$$\sum_{i=1}^{N_L} P_{D_j}^{final} = \sum_{i=1}^{N_G} P_{G_i}^{final} = 8949 \ MW$$

- A power generation dispatch based on both hydraulic and thermal plants
- The three generation power dispatches are considered and compared

Day 2 characterized by:

• A lower power demand level

 $\sum_{i=1}^{N_L} P_{D_j}^{final} = \sum_{i=1}^{N_G} P_{G_i}^{final} = 7598 MW$

- A more hydraulic based power generation dispatch
- Only "Ideal" and "Coordinated" generation power dispatches are considered and compared

No generation power re-dispatch is considered (i.e. maximal generation power limit is set equal to the initial generation dispatch)

No line maximal transmission capacity constraints are considered during cascade phenomena



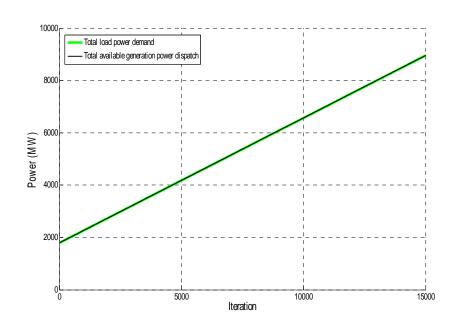
DC SPFM input parameters setting

Day 1 with higher power demand level and N-k contingencies

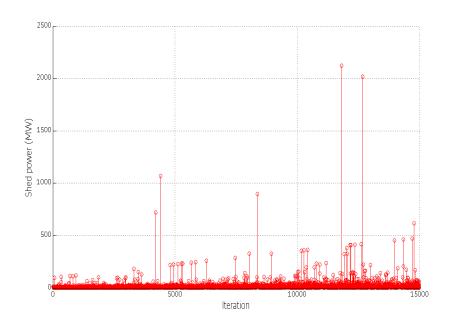
"Network Dispatch" issued from Colombian TSO database

λ : not used (linear variations of power demand)	$lpha_k=1$	eta = 100 κ = 2 % (not be used in day-ahead analysis)	
$\Delta P_{D}^{\mathrm{min}} = 0.01 \% \ of \ \sum_{j=1}^{N_L} P_{D_j}$	$\Delta P_{\rm G}^{ m min}=0$ (no generation power re-dispatch is allowed)		
$\mu_i = 1.05$	$\mu_a = 1.50$	$\tau_a = 150 iterations$	
$p_{f_r}^0 = 0.0015$ for $r \in \begin{bmatrix} 1 & \cdots & N_B \end{bmatrix}$	$p_{f_r}^1 = f(L_r)$	$\mathcal{L}_r^{th} = 0.99$ for $r \in \begin{bmatrix} 1 & \cdots & N_{\scriptscriptstyle B} \end{bmatrix}$	
$r_p = 5$	$r_T = 5$	$Nb_{ter} = 15000$	



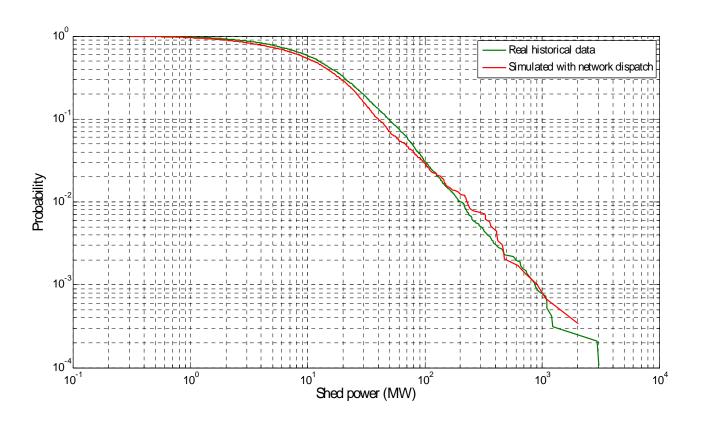


Evolution of total load power demand and total available generation power (SOC process)



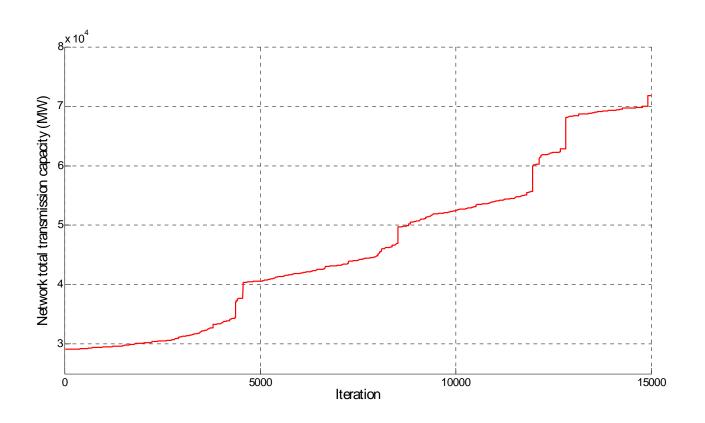
Distribution of shed power demand (N-k) contingency, "network dispatch)





CDF of shed power demand



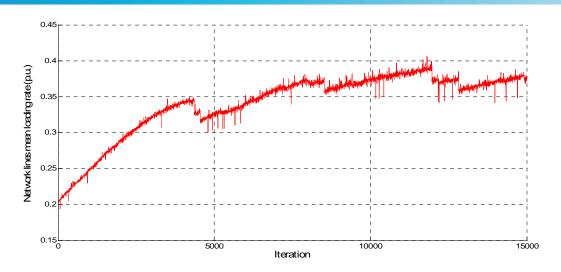


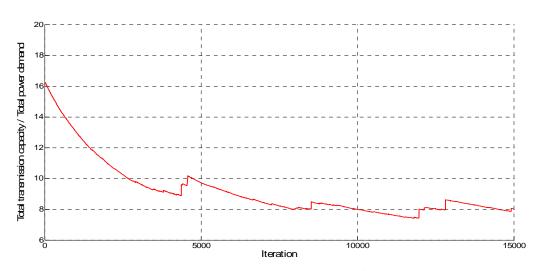
Network total transmission capacity (SOC process)



Evolution of network lines mean loading rate (SOC parameter τ)

Evolution of the ratio total transmission capacity over total power demand (SOC parameter γ)

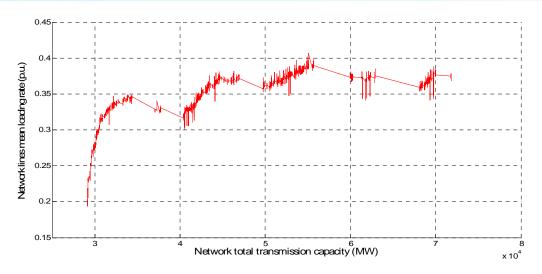


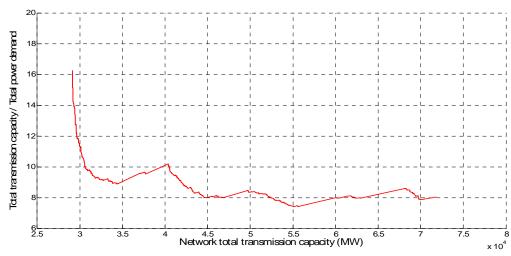




Normalized evolution of network lines mean loading rate (τ) / network total transmission capacity

Normalized evolution of the ratio total transmission capacity over total power demand (γ) / network total transmission capacity

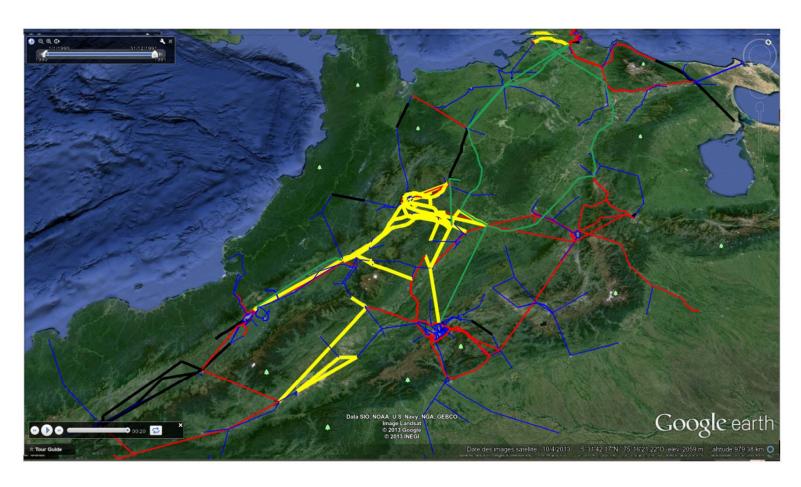






Cascading phenomena

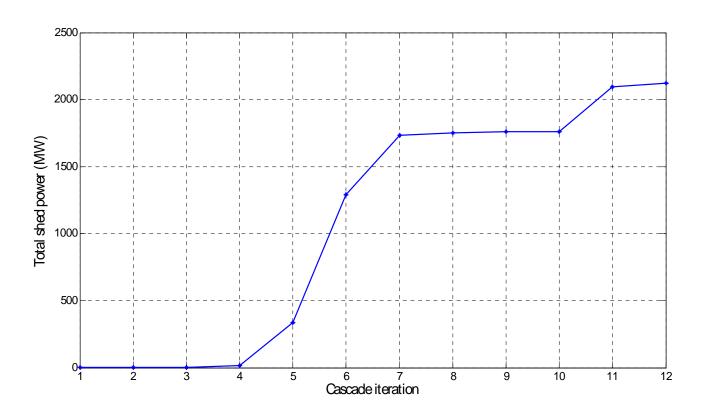
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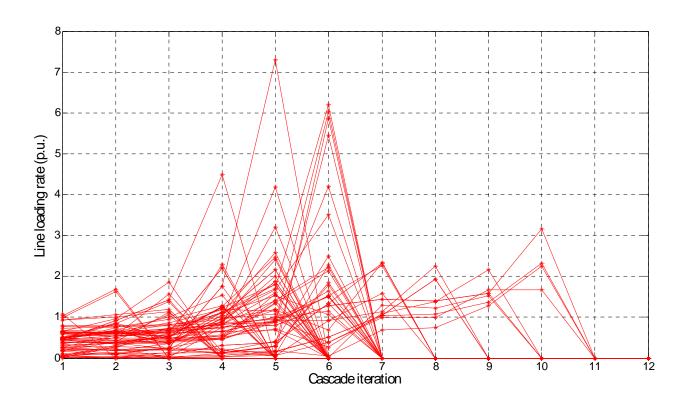
Particular case: Iteration 11815

$$\Delta P_D = 2121MW$$



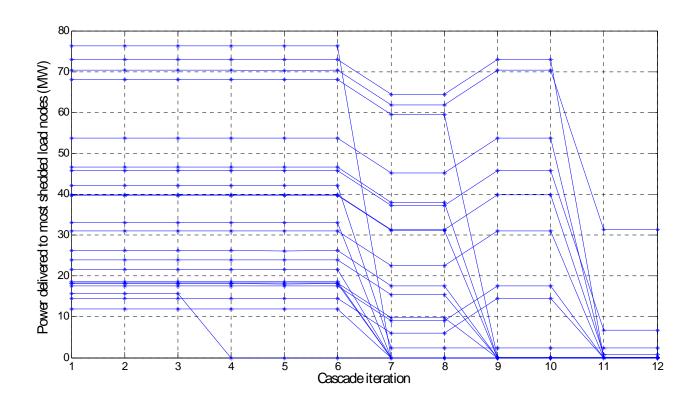
Evolution of network total shed power demand during cascade sequence





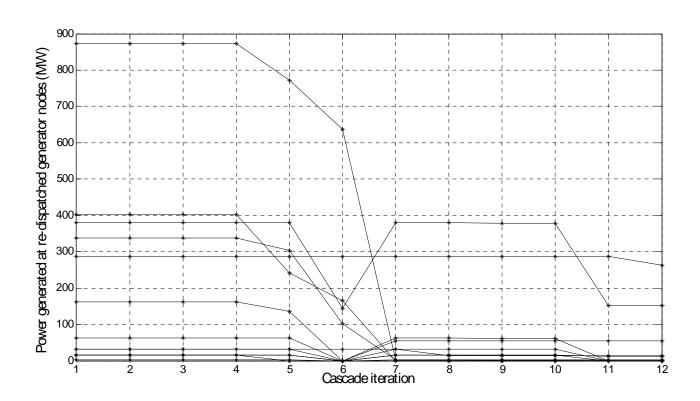
Evolution of loading rate of lines tripped during cascade sequence





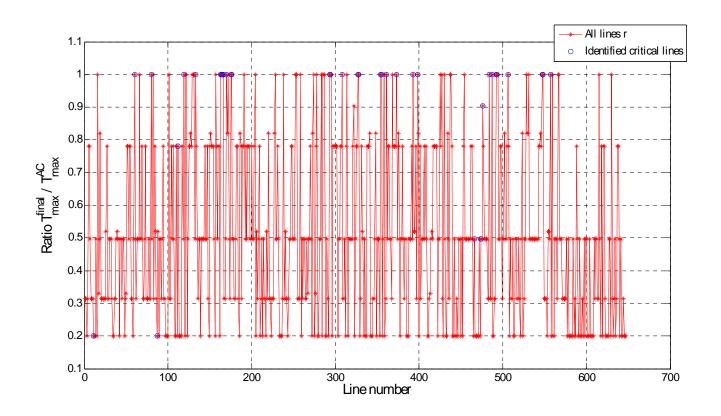
Evolution of power delivered to most shed load nodes: $\Delta P_{D_i} \ge 10MW$





Evolution of generation power produced at each re-dispatched generator nodes





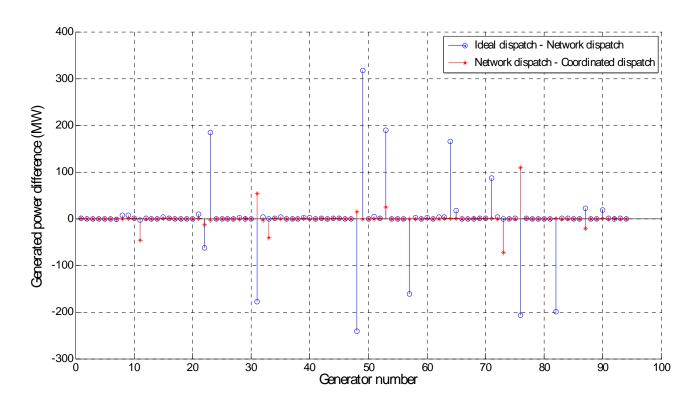
Evolution of the ratio $T_{
m max}^{
m \it final}$ / $T_{
m max}^{
m \it AC}$ for each line



| Line number |
|-------------|-------------|-------------|-------------|-------------|-------------|
| 11 | 133 | 175 | 328 | 398 | 492 |
| 60 | 163 | 176 | 354 | 466 | 493 |
| 80 | 164 | 293 | 355 | 474 | 506 |
| 87 | 165 | 294 | 361 | 476 | 547 |
| 112 | 166 | 308 | 373 | 484 | 548 |
| 119 | 170 | 327 | 393 | 487 | 557 |

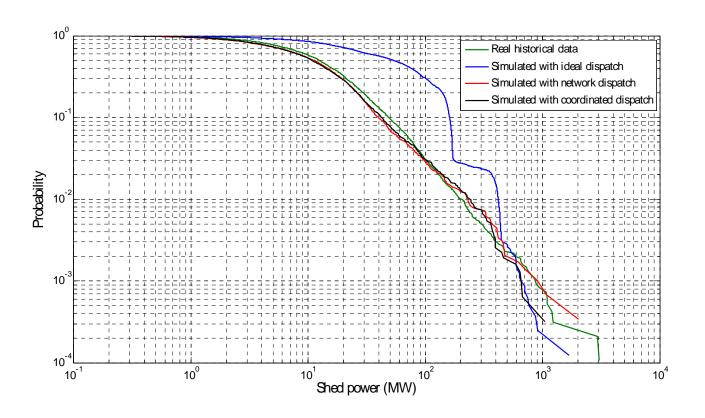


Comparison of the three dispatches



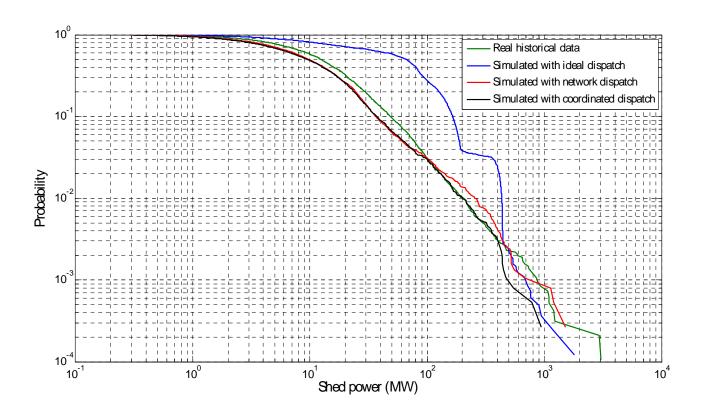
- 11.9% generated power modification from "Ideal" to "Network"
- 2.3% generated power modification from "Network" to "Coordinated"





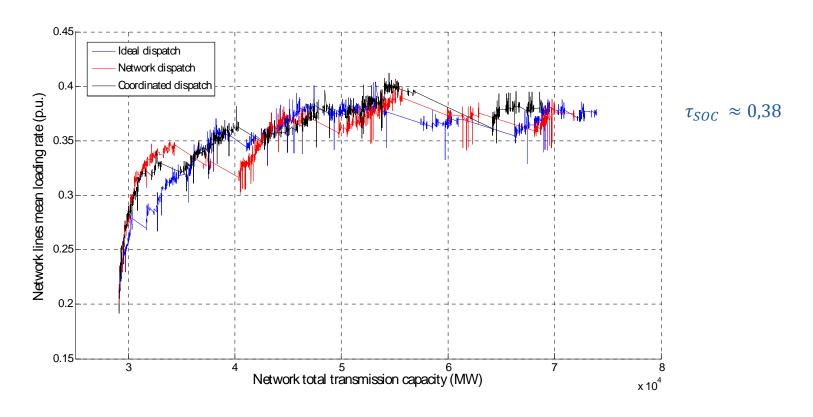
Comparison of shed load power demand distributions: N-k contingencies





Comparison of shed load power demand distributions: N-1 contingencies



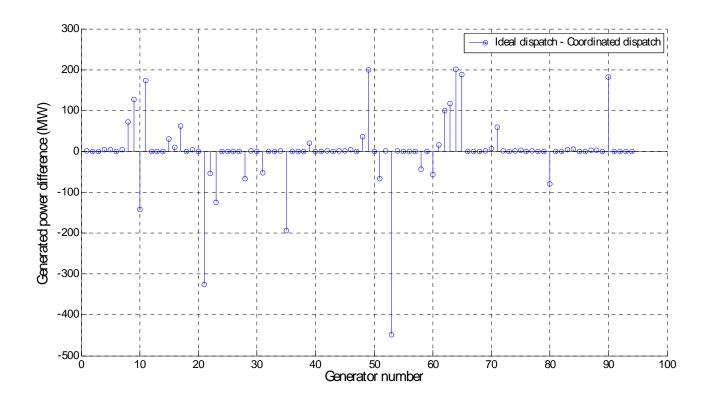


Comparison of SOC condition characteristics parameters



Day 2: Day-ahead successive generation dispatches

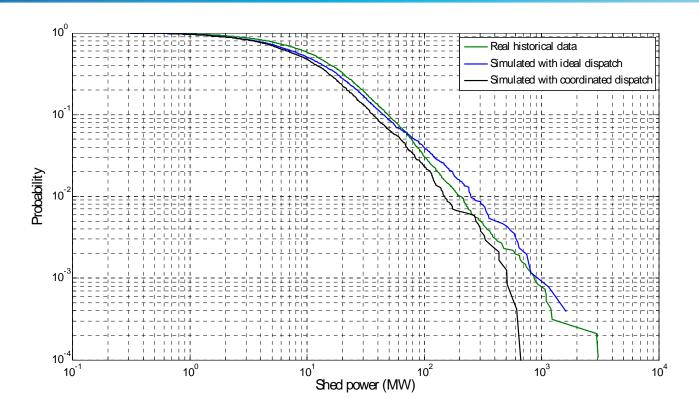
Comparison of the two dispatches



21.8% generated power modification from "Ideal" to "Coordinated"



Day 2: Day-ahead successive generation dispatches



Comparison of shed load power demand distributions: N-k contingencies

٦	Line number					
	27	82	227	318	398	476
	29	125	308	327	418	507
	67	165	313	361	473	630



